

Welcome Back!

	Assignment Effort Grade (Circle One)	Comments (What was interesting or challenging?)
Monday Date: <u>2/26</u> Topic: <u>Exponential Project Due!</u>	0 1 2	
Tuesday Date: <u>2/27</u> Topic: <u>ACT For Juniors</u>	0 1 2	
Wednesday Date: <u>2/28</u> Topic: <u>Finish project or add problems to study guide</u>	0 1 2	
Thursday Date: _____ Topic: _____	0 1 2	
Friday Date: _____ Topic: _____	0 1 2	

Warm-up: $y = 500(1.002)^x$

Miles deposited \$500 into a bank account with .2% annual interest.

Predict his investment after 3 years.

3 Years, \$500, .2% $1+r = 1 + .002$

$$y = 500(1.002)^x$$

$$y = 500(1.002)^3$$

$$y \approx 500(1.006)$$

$$y \approx \$503$$

Class Plan:

1. Warm-up



2. Review: **Trashketball! :)**

-Properties of exponents

-Growth/Decay applications

Recall the Properties of Indices

$$b^m \cdot b^n = b^{m+n}$$

$$(b^m)^n = b^{m \cdot n}$$

$$(ab)^n = a^n \cdot b^n$$

$$\frac{b^m}{b^n} = b^{m-n}$$

$$b^{-n} = \frac{1}{b^n}$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

$$b^0 = 1$$

Recall our Exponential Equation:

a: Starting value $y = a \cdot b^x$

b: Constant multiplier (multiplier is always positive.)

r: Rate of growth/decay, interpreted as a %

Exponential Growth

$$b > 1$$

$$y = a(1 + r)^x$$

Ant Population Example:

$$y = 16(1.5)^x$$

r = 50% growth

Exponential Decay

$$0 < b < 1$$

$$y = a(1 - r)^x$$

Car Value Example:

$$y = 21,700(0.83)^x$$

r = 17% depreciation

Trashketball

Table 1

|||||

WIN

Table 2

|||

Table 3

|||

Table 4

||

Table 5

||||

Table 6

|||||

Table 7

Table 8

Table 9

Trashketball

1. Work together to put 1 solution on your board, **wait** to hold it up until told.
2. Table correct? **1 point.**
3. Every 2 points, a person from the **table** gets to shoot for 1, 2 or 3 bonus points
4. Teacher is the judge - if you are taking too long - or losing focus - you lose your shot :) Stay on your game!



Property Examples:

Simplify. Your answer should contain only positive exponents.

1) $4x^1 \cdot 2x^2 = 8x^3$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

2) $(4^3)^{-2}$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

3) $(2p^{-1})^3$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$4) \frac{k^{-3}}{4k^0} = \frac{k^{-3}}{4} = \frac{1}{4k^3}$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$5) \frac{3n^0}{2n^4 \cdot 3n}$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$6) m \cdot (m^{-2})^3 = m^1 \cdot m^{-6} = m^{-5} = \frac{1}{m^5}$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$7) \frac{2x^3}{(x^{-1})^3} = \frac{2 \cdot x \cdot x \cdot x}{(x^{-1})(x^{-1})(x^{-1})} = \frac{2x^3}{x^{-3}} = \boxed{2x^6}$$

$\rightarrow \frac{2x^3}{x^{-3}} \rightarrow$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$8) (2m)^3 \cdot (2m^{-3}n^{-2})^4$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
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Property Examples:

Simplify. Your answer should contain only positive exponents.

$$9) \frac{(x^{-4}y^3)^4}{2x}$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Simplify. Your answer should contain only positive exponents.

$$10) \frac{2m^0 \cdot 3m^4 n^{-3}}{2n^4}$$

$b^m \cdot b^n = b^{m+n}$	$(b^m)^n = b^{m \cdot n}$	$(ab)^n = a^n \cdot b^n$	$b^0 = 1$
$\frac{b^m}{b^n} = b^{m-n}$	$b^{-n} = \frac{1}{b^n}$	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	

Property Examples:

Solutions!

1) $8x^3$

2) $\frac{1}{4^6}$

3) $\frac{8}{p^3}$

4) $\frac{1}{4k^3}$

5) $\frac{1}{2n^5}$

6) $\frac{1}{m^5}$

7) $2x^6$

8) $\frac{128}{m^9 n^8}$

9) $\frac{y^{12}}{2x^{17}}$

10) $\frac{3m^4}{n^7}$

Growth and Decay Applications

$$T = 80(.913)^t$$

Equation represents the temperature (C)
of a cup of tea t minutes after it was heated.



11) What was the initial temperature of the tea?

Growth and Decay Applications

$$T = 80(.913)^t$$

Equation represents the temperature (C) of a cup of tea t minutes after it was heated.



11) What was the initial temperature of the tea?

The temperature when the tea was poured was 80°C .

$P = 815(1.16)^{12}$
 $P \approx 815(5.936)$
 $P \approx 4838 \text{ zebras!}$

Growth and Decay Applications

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12) Find the temperature after 12 minutes. **Show work!**

Growth and Decay Applications

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Equation represents the temperature (C) of a cup of tea t minutes after it was heated.



12) Find the temperature after 12 minutes. **Show work!**

$$T = 80(.913)^{12}$$
$$T \approx 80(.335)$$

$$T \approx 26.84^\circ\text{C}$$

Growth and Decay Applications

$$T = 80(.913)^t$$

Equation represents the temperature (C) of a cup of tea t minutes after it was heated.



13) Enter the equation into your graphing calculator. [$y = 80(.913)^x$]

Determine when the temperature will fall below 30 C.

```
Plot1 Plot2 Plot3
Y1=80(.913)^X
Y2=
Y3=
```

X	Y1	
12	26.837	
13	24.502	
14	22.371	
15	20.425	
16	18.648	
17	17.025	
18	15.544	

X=12

Growth and Decay Applications

$$T = 80(.913)^t$$

Equation represents the temperature (C) of a cup of tea t minutes after it was heated.



13) Enter the equation into your graphing calculator. [$y = 80(.913)^x$]

Determine when the temperature will fall below 30 C.

The table shows that after **11** minutes, the temperature will drop below 30° C.

```
Plot1 Plot2 Plot3
Y1=80(.913)^X
Y2=
Y3=
```

X	Y1	
12	26.837	
13	24.502	
14	22.371	
15	20.425	
16	18.648	
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X=12

Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



14) At what percentage rate is the zebra population growing?

Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



14) At what percentage rate is the zebra population growing?

The growth rate is 0.16, or 16%.

$[(1 + r) = 1.16, \text{ or } 1 + .16]$

Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



15) Predict the population of zebras after 12 years. **Show work!**

Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



15) Predict the population of zebras after 12 years. **Show work!**

Handwritten work on a piece of paper:

$$P = 815(1.16)^{12}$$
$$P \approx 815(5.936)$$
$$P \approx 4838 \text{ zebras!}$$

Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



16) Predict the population of zebras after 18 years. **Show work!**

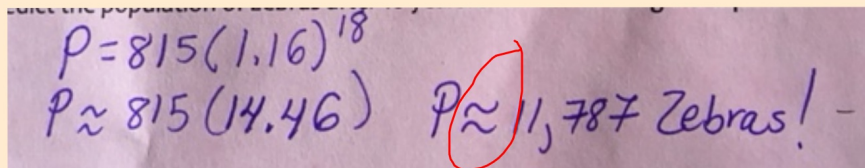
Growth and Decay Applications

$$P = 815(1.16)^t$$

Equation shows the population (P) of zebras, t years after an initial count.



16) Predict the population of zebras after 18 years. **Show work!**

Handwritten work on a piece of paper. The first line shows the equation $P = 815(1.16)^{18}$. The second line shows the calculation $P \approx 815(14.46)$. The final result $P \approx 11,787$ Zebras! is circled in red.

$P = 815(1.16)^{18}$
 $P \approx 815(14.46)$ $P \approx 11,787$ Zebras! -