

Assignment Self-Monitoring Sheet

	Assignment Effort Grade (Circle One)	Comments (What was interesting or challenging?)
Monday Date: <u>9/18</u> Topic: <u>Movie Ticket Analysis</u>	0 1 2	
Tuesday Date: <u>9/19</u> Topic: <u>HowOld.net Analysis</u>	0 1 2	
Wednesday Date: <u>9/20</u> Topic: <u>No homework - yesterday was a quiz.</u>	0 1 2	
Thursday Date: <u>9/21</u> Topic: <u>Pre Read: Ch. 19 Section A</u>	0 1 2	
Friday Date: _____ Topic: _____	0 1 2	

Warm-up:

What did you learn when you read Chapter 19 Section A?

A Chapter 19 **GRAPHICAL SOLUTION**

Certain solutions of lines
 types of lines parallel
 # of solutions

How do we graph lines?

1 Method: Plot y-intercept, use gradient to find another point

Class Plan

1. Warm-up

2. Graphing Systems of Equations (Textbook 19A)

*What does a solution look like?

3. Joke Break :)

4. Practice

Recall Prior Knowledge...

F Chapter 8 GRAPHING LINES FROM EQUATIONS

GRAPHING LINES IN GRADIENT-INTERCEPT FORM

To draw the graph of $y = mx + c$ we:

- Use the y -intercept c to plot the point $(0, c)$.
- Use x and y -steps from the gradient m to locate another point on the line.
- Join the two points and extend the line in either direction.

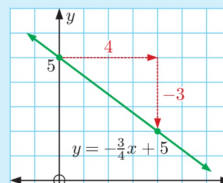
Example 14

Self

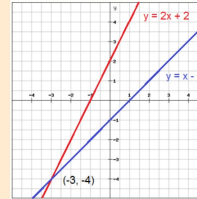
Draw the graph of $y = -\frac{3}{4}x + 5$.

For $y = -\frac{3}{4}x + 5$:

- the y -intercept is $c = 5$
- the gradient is $m = -\frac{3}{4}$ \leftarrow y -step
 \leftarrow x -step



If we graph two lines (equations),
what could it look like?



Find the intersection!
Do lines always intersect?

A

Chapter 19

GRAPHICAL SOLUTION

One way to solve simultaneous equations is to draw the graph of both equations on the same set of axes. The **point of intersection** corresponds to a solution to the simultaneous equations.

A set of two linear simultaneous equations can have either one, zero, or infinitely many solutions.

intersecting lines



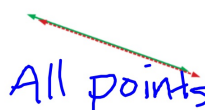
one solution

parallel lines



no solutions

coincident lines



infinitely many solutions

$$\begin{cases} y = 2x + 3 \\ y = -x + 9 \end{cases}$$

Solution (2, 7)

$$\begin{cases} y = \frac{3}{4}x + 3 \\ y = \frac{3}{4}x + 9 \end{cases}$$

Same slopes!

$$\begin{cases} 2y = -6x + 8 \\ y = -3x + 4 \end{cases}$$

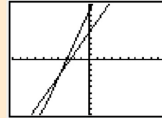
Same equation!

Solving System of Equations

3 Possible Types of Solutions

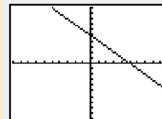
1. One Solution

One intersection on the graph



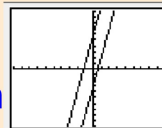
2. Infinite Solutions

Uncountable intersections on the graph



3. No Solution

No intersection on the graph



Solving System of Equations

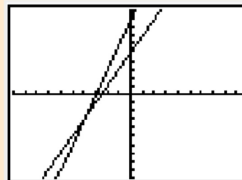
3 Possible Types of Solutions

1. One Solution

One intersection on the graph

$$y = 2x + 5$$
$$y = 3x + 9$$

ex. $x = -4, y = -3$



Solving System of Equations

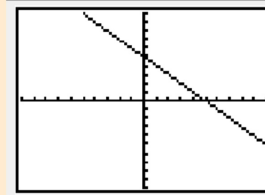
3 Possible Types of Solutions

2. Infinite Solutions

Uncountable intersections

$$\begin{aligned}y &= -x + 5 \\y &= 5 - x\end{aligned}$$

TRUE statement is
result ex. $0 = 0$.



Solving System of Equations

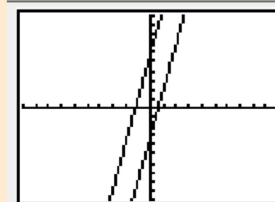
3 Possible Types of Solutions

3. No Solution

No intersection on the graph

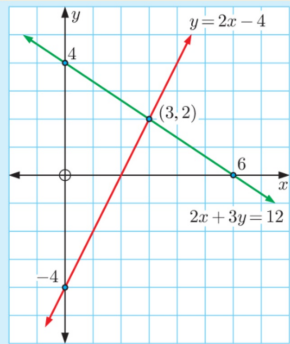
$$\begin{aligned}y &= 5x - 3 \\y &= 5x + 6\end{aligned}$$

FALSE statement
is the result
ex. $9 = 0$.



Example 1

Solve the following simultaneous equations graphically: $\begin{cases} y = 2x - 4 \\ 2x + 3y = 12 \end{cases}$



We draw the graphs of $y = 2x - 4$ and $2x + 3y = 12$ on the same set of axes.

The graphs meet at the point $(3, 2)$.

\therefore the solution is $x = 3, y = 2$.

Check:

Substituting these values into:

- $y = 2x - 4$ gives $2 = 2(3) - 4$ ✓
- $2x + 3y = 12$ gives $2(3) + 3(2) = 12$ ✓

Joke Break :)

Parallel lines
have so much in
common...

it's a shame that
they'll never
meet.

$(x+a)(x-i)$

PLAN
 ~~$(P+L)(A+N)$~~
 $PA+PN+LA+LN$

Your plan has been
foiled

Investigation:

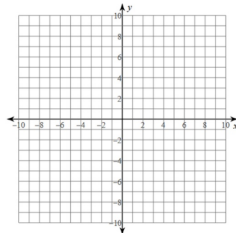
A

GRAPHICAL SOLUTION

Solutions to Systems of Equations

- *Identify gradient/slope (m) & y-intercept (c)
- *Graph equations
- *Find intersection(solution)!

Directions: Graph the following systems of equations.



$$\begin{cases} y = \frac{1}{3}x - 1 \\ y = -2x + 6 \end{cases}$$

Line 1:
Gradient: _____
Y-intercept: _____

Line 2:
Gradient: _____
Y-intercept: _____

Solution: _____



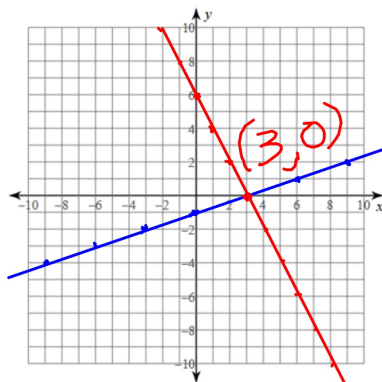
Done? Show teacher and start practice

A

Investigation

GRAPHICAL SOLUTION

Directions: Graph the following systems of equations.



$$\begin{cases} y = \frac{1}{3}x - 1 \text{ ①} \\ y = -2x + 6 \text{ ②} \end{cases}$$

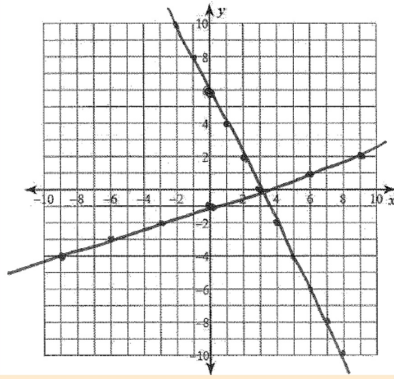
Line 1:
Gradient: $\frac{1}{3}$ $\frac{\text{up } 1}{\text{r} + 3}$
Y-Intercept: -1

Line 2:
Gradient: -2 $\frac{\text{dn } 2}{\text{r} + 1}$
Y-Intercept: 6

Solution: $(3, 0)$

A**Solution****GRAPHICAL SOLUTION**

Directions: Graph the following systems of equations.



$$\begin{cases} y = \frac{1}{3}x - 1 & \textcircled{1} \\ y = -2x + 6 & \textcircled{2} \end{cases}$$

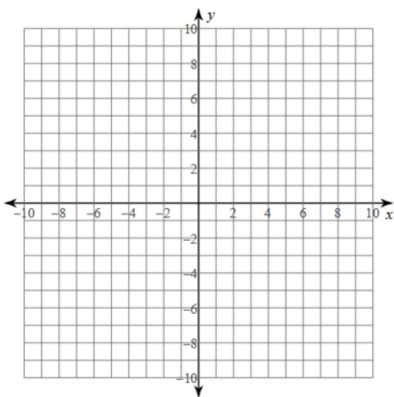
Line 1:
Gradient: $\frac{1}{3}$ $\frac{\text{up } 1}{\text{right } 3}$

Y-Intercept: -1

Line 2:
Gradient: -2 $\frac{\text{dn } 2}{\text{r } 1}$

Y-Intercept: 6

Solution: $(3, 0)$

A**Investigation****GRAPHICAL SOLUTION**

Graph both equations.

$$\begin{cases} y = -\frac{2}{5}x + 1 \\ y = -\frac{2}{5}x - 3 \end{cases}$$

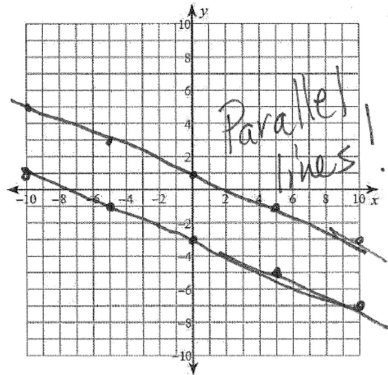
Line 1:
Gradient: _____

Y-Intercept: _____

Line 2:
Gradient: _____

Y-Intercept: _____

Solution: _____

A**Solution****GRAPHICAL SOLUTION**

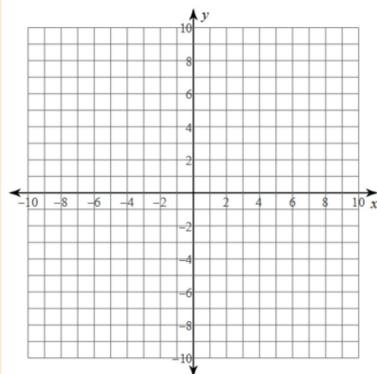
Graph both equations.

$$\begin{cases} y = -\frac{2}{5}x + 1 & \textcircled{1} \\ y = -\frac{2}{5}x - 3 & \textcircled{2} \end{cases}$$

Line 1: $-\frac{2}{5} = \frac{\Delta y}{\Delta x} = \frac{\Delta y}{\Delta x}$
 Gradient: $\frac{-2}{5}$ (left 5, up 2)

Y-Intercept: 1

Line 2:
 Gradient: $-\frac{2}{5}$

Y-Intercept: -3Solution: NO SOLUTION!**A****Investigation****GRAPHICAL SOLUTION**

Graph both equations.

$$\begin{cases} y = 2x + 4 \\ -2x + y = 4 \end{cases}$$

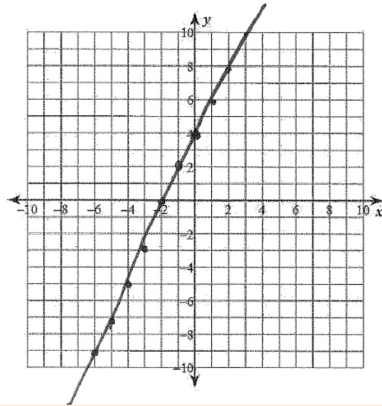
Line 1:
 Gradient: _____

Y-Intercept: _____

Line 2:
 Gradient: _____

Y-Intercept: _____

Solution: _____

A**Solution****GRAPHICAL SOLUTION**

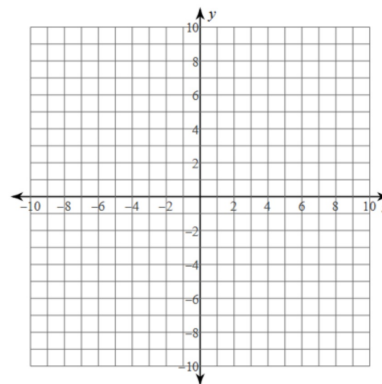
Graph both equations.

$$\begin{cases} y = 2x + 4 & \textcircled{1} \\ -2x + y = 4 & \textcircled{2} \end{cases}$$

Line 1:
 Gradient: $2 \frac{\text{up } 2}{\text{right } 1}$
 Y-Intercept: 4

Line 2:
 Gradient: $2 \frac{\text{down } 2}{\text{left } 1}$
 Y-Intercept: 4

Solution: All points on the line

A**Investigation****GRAPHICAL SOLUTION****Challenge Problem!**

Graph both equations.

$$\begin{cases} x + 2y = 6 \\ 5x + 2y = -2 \end{cases}$$

Line 1:
 Gradient: _____
 Y-Intercept: _____

Line 2:
 Gradient: _____
 Y-Intercept: _____

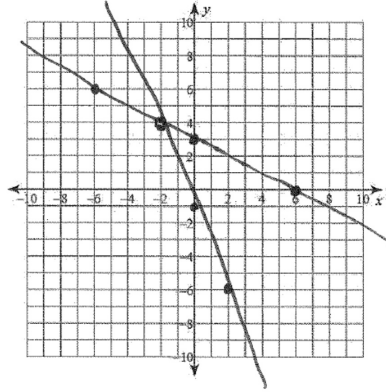
Solution: _____

A

Solution

GRAPHICAL SOLUTION

Challenge Problem!



Using intercepts

Graph both equations.

$$\begin{cases} x+2y=6 & x=6, y=3 \\ 5x+2y=-2 & x=-\frac{2}{5}, y=-1 \\ y=-\frac{5}{2}x-1 \end{cases}$$

Line 1:
Gradient: _____

Y-Intercept: _____

Line 2:
Gradient: _____

Y-Intercept: _____

Solution: $(-2, 4)$

A

Chapter 19

GRAPHICAL SOLUTION

19A.1 (Page 375)

Exercises: #1 and #3

EXERCISE 19A.1

1 Solve the following simultaneous equations graphically:

a $\begin{cases} y = 4x - 1 \\ y = 2x - 3 \end{cases}$

b $\begin{cases} y = 3x \\ y = -2x + 5 \end{cases}$

c $\begin{cases} y = x + 2 \\ y = -3x - 6 \end{cases}$

Slope -
y-int -

3 Try to solve the following simultaneous equations graphically. State the number of solutions in each case.

a $\begin{cases} y = 4x + 1 \\ y = 4x - 3 \end{cases}$

b $\begin{cases} x - \frac{1}{2}y = -3 \\ y = 2x + 6 \end{cases}$

c $\begin{cases} 5x + 3y = 2 \\ 5x + 3y = -7 \end{cases}$

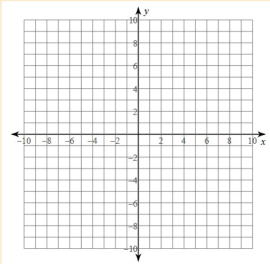
EXERCISE 19A.1

1 Solve the following simultaneous equations graphically:

a
$$\begin{cases} y = 4x - 1 \\ y = 2x - 3 \end{cases}$$

b
$$\begin{cases} y = 3x \\ y = -2x + 5 \end{cases}$$

c
$$\begin{cases} y = x + 2 \\ y = -3x - 6 \end{cases}$$

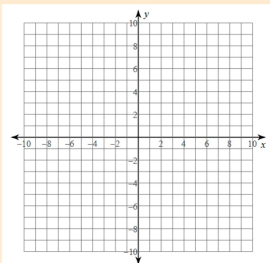


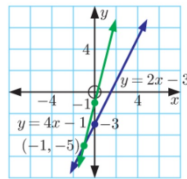
3 Try to solve the following simultaneous equations graphically. State the number of solutions in each case.

a
$$\begin{cases} y = 4x + 1 \\ y = 4x - 3 \end{cases}$$

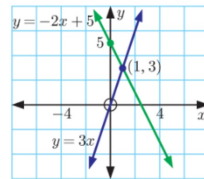
b
$$\begin{cases} x - \frac{1}{2}y = -3 \\ y = 2x + 6 \end{cases}$$

c
$$\begin{cases} 5x + 3y = 2 \\ 5x + 3y = -7 \end{cases}$$

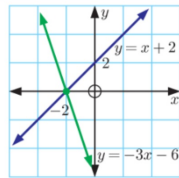


A**SOLUTIONS!****GRAPHICAL SOLUTION****EXERCISE 19A.1****1 a**

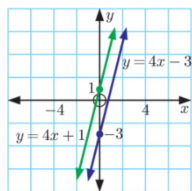
$$x = -1, \quad y = -5$$

b

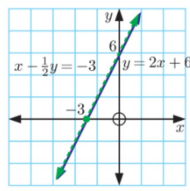
$$x = 1, \quad y = 3$$

c

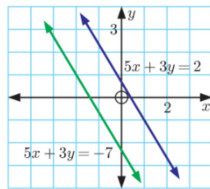
$$x = -2, \quad y = 0$$

A**SOLUTIONS!****GRAPHICAL SOLUTION****3 a**

No solutions, the lines are parallel.

b

Infinitely many solutions, the lines are coincident.

c

No solutions, the lines are parallel.