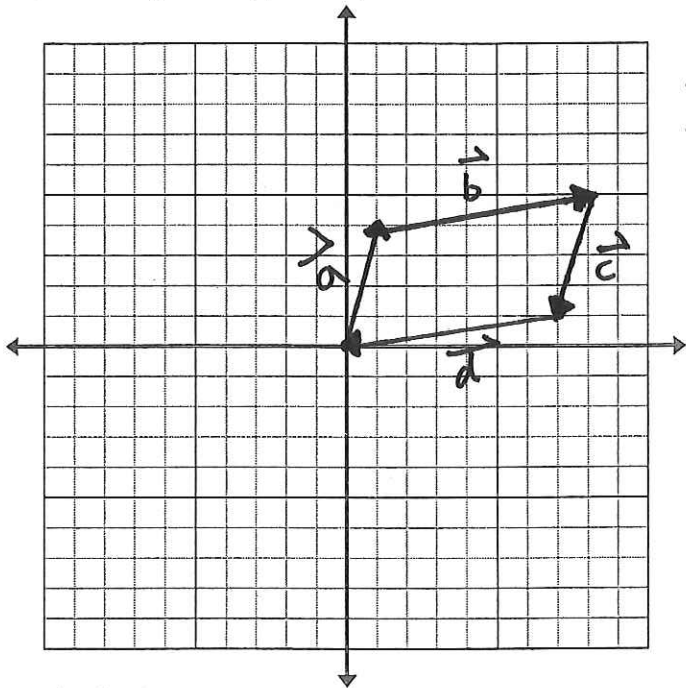


SHOW ALL OF YOUR WORK.

a) Graph vectors $\vec{a} + \vec{b} + \vec{c} + \vec{d}$ when $\vec{a} = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 7 \\ 1 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} -1 \\ -4 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -7 \\ -1 \end{pmatrix}$ on the graph below.

b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.

c) Classify the type of quadrilateral.



After making calculations, identify properties below:

$|\vec{a}| = |\vec{c}|$ Opposite vectors are equal.

$|\vec{b}| = |\vec{d}|$ Opposite sides are equal.

No vectors are orthogonal, so no sides meet at 90° .

$\vec{a} \parallel \vec{c}$ Opposite sides are parallel.

$\vec{b} \parallel \vec{d}$

Quadrilateral

Parallelogram

Calculations

Magnitudes (lengths):

$$|\vec{a}| = \sqrt{1^2 + 4^2} = \sqrt{1 + 16} = \sqrt{17}$$

$$|\vec{b}| = \sqrt{7^2 + 1^2} = \sqrt{49 + 1} = \sqrt{50}$$

$$|\vec{c}| = \sqrt{(-1)^2 + (-4)^2} = \sqrt{1 + 16} = \sqrt{17}$$

$$|\vec{d}| = \sqrt{(-7)^2 + (-1)^2} = \sqrt{49 + 1} = \sqrt{50}$$

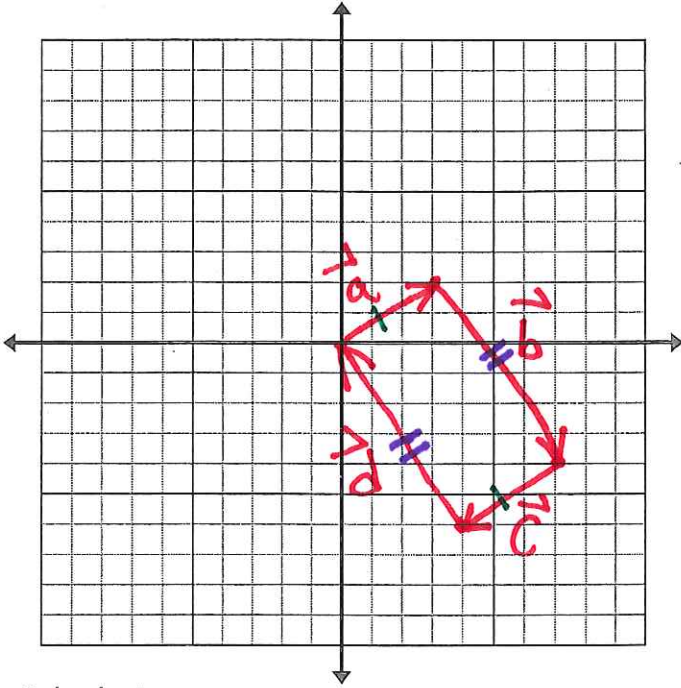
Parallel or Perpendicular Vectors:

$$\left. \begin{array}{l} \vec{a} \cdot \vec{b} \neq 0 \\ \vec{b} \cdot \vec{c} \neq 0 \\ \vec{c} \cdot \vec{d} \neq 0 \\ \vec{d} \cdot \vec{a} \neq 0 \end{array} \right\} \text{No orthogonal vectors}$$

$$\left. \begin{array}{l} \vec{a} = -\vec{c} \\ \vec{b} = -\vec{d} \end{array} \right\} \text{Parallel Vectors}$$

SHOW ALL OF YOUR WORK.

- a) Graph vectors $\vec{a} + \vec{b} + \vec{c} + \vec{d}$ when $\vec{a} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 4 \\ -6 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} -3 \\ -2 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -4 \\ 6 \end{pmatrix}$ on the graph below.
- b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.
- c) Classify the type of quadrilateral.



After making calculations, identify properties below:

2 pairs of congruent magnitudes
(opposite sides are \cong)

4 orthogonal vectors that form 4 right angles.

Quadrilateral

Rectangle

Calculations

Magnitudes (lengths):

$$|\vec{a}| = \sqrt{9+4} = \sqrt{13}$$

$$|\vec{b}| = \sqrt{16+36} = \sqrt{52} = 2\sqrt{13}$$

$$|\vec{c}| = \sqrt{9+4} = \sqrt{13}$$

$$|\vec{d}| = \sqrt{16+36} = \sqrt{52} = 2\sqrt{13}$$

Equal size

Equal size

Parallel or Perpendicular Vectors:

$$\begin{matrix} \vec{b} \\ \vec{d} \end{matrix} = -\begin{matrix} \vec{c} \\ \vec{a} \end{matrix} \left. \vphantom{\begin{matrix} \vec{b} \\ \vec{d} \end{matrix}} \right\} \text{Parallel Vectors!}$$

$$\vec{a} \cdot \vec{b} = 3(4) + 2(-6) = 0$$

$$\vec{b} \cdot \vec{c} = 4(-3) + -2(-6) = 0$$

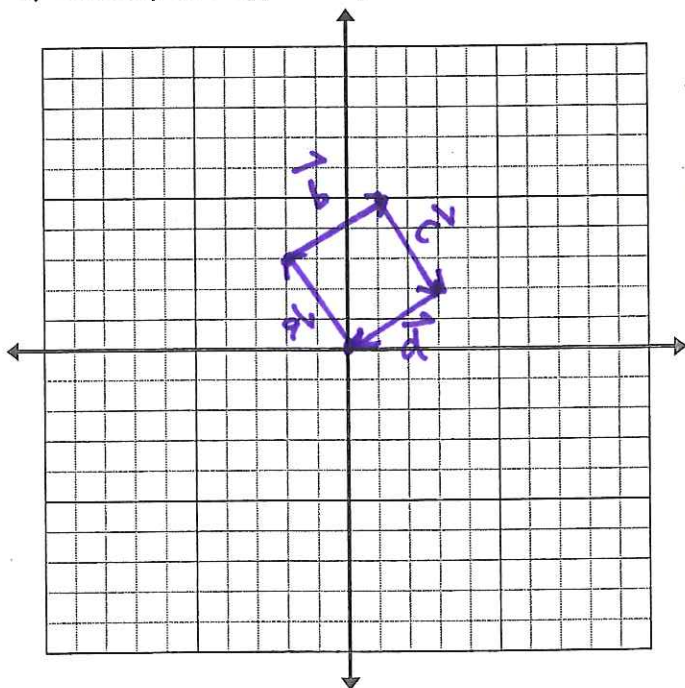
$$\vec{c} \cdot \vec{d} = -3(-4) + -2(6) = 0$$

$$\vec{d} \cdot \vec{a} = -4(3) + 6(2) = 0$$

orthogonal
vectors

SHOW ALL OF YOUR WORK.

- a) Graph vectors $A+B+C+D$ when $\vec{a} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -3 \\ -2 \end{pmatrix}$ on the graph below.
- b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.
- c) Classify the type of quadrilateral.



After making calculations, identify properties below:

$|\vec{a}| = |\vec{b}| = |\vec{c}| = |\vec{d}|$ All sides are equal.

$\vec{a} \perp \vec{b}$
 $\vec{b} \perp \vec{c}$
 $\vec{c} \perp \vec{d}$
 $\vec{d} \perp \vec{a}$

Each vector is perpendicular to the next.
 Sides meet at 90° angles.

$\vec{a} \parallel \vec{c}$
 $\vec{b} \parallel \vec{d}$

Opposite sides are parallel

Quadrilateral
 Square

Calculations

Magnitudes (lengths):

$|\vec{a}| = \sqrt{(-2)^2 + 3^2} = \sqrt{4 + 9} = \sqrt{13}$
 $|\vec{b}| = \sqrt{3^2 + 2^2} = \sqrt{9 + 4} = \sqrt{13}$
 $|\vec{c}| = \sqrt{2^2 + (-3)^2} = \sqrt{4 + 9} = \sqrt{13}$
 $|\vec{d}| = \sqrt{(-3)^2 + (-2)^2} = \sqrt{9 + 4} = \sqrt{13}$

Parallel or Perpendicular Vectors:

$\vec{a} \cdot \vec{b} = -2(3) + 3(2) = -6 + 6 = 0$
 $\vec{b} \cdot \vec{c} = 3(2) + 2(-3) = 6 - 6 = 0$
 $\vec{c} \cdot \vec{d} = 2(-3) + (-3)(-2) = -6 + 6 = 0$
 $\vec{d} \cdot \vec{a} = -3(-2) + (-2)(3) = 6 - 6 = 0$
 $\vec{a} \cdot \vec{c} = -2(2) + 3(-3) = -4 - 9 = -13$
 $\vec{b} \cdot \vec{d} = 3(-3) + 2(-2) = -9 - 4 = -13$

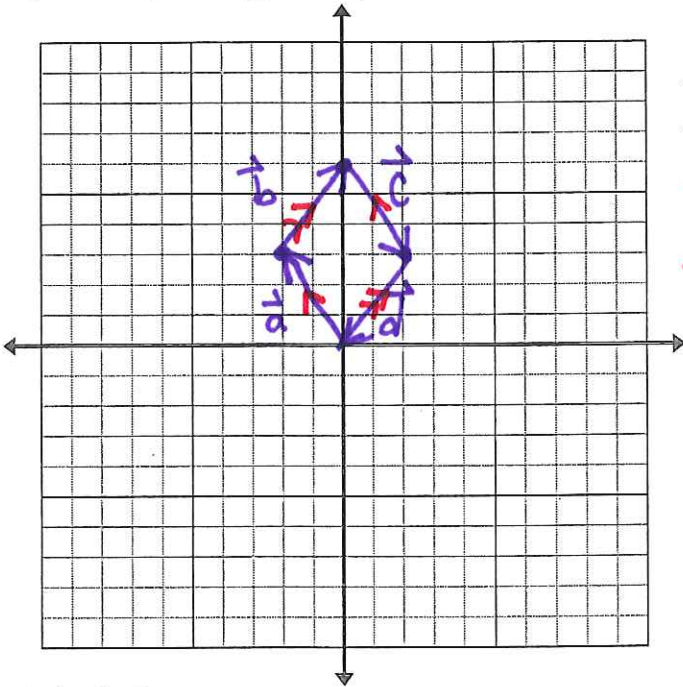
$\vec{a} = -\vec{c}$
 $\vec{b} = -\vec{d}$ } Parallel Vectors

SHOW ALL OF YOUR WORK.

a) Graph vectors $\vec{A} + \vec{B} + \vec{C} + \vec{D}$ when $\vec{a} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$ on the graph below.

b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.

c) Classify the type of quadrilateral.



After making calculations, identify properties below:

- 2 pairs of parallel vectors
 - 4 congruent magnitudes
- Equilateral Parallelogram!

Quadrilateral

RHOMBUS

Calculations

Magnitudes (lengths):

$$|\vec{a}| = \sqrt{4 + 9} = \sqrt{13}$$

$$|\vec{b}| = \sqrt{4 + 9} = \sqrt{13}$$

$$|\vec{c}| = \sqrt{4 + 9} = \sqrt{13}$$

$$|\vec{d}| = \sqrt{4 + 9} = \sqrt{13}$$

Parallel or Perpendicular Vectors:

$$\left. \begin{array}{l} \vec{a} \cdot \vec{b} \neq 0 \\ \vec{b} \cdot \vec{c} \neq 0 \\ \vec{c} \cdot \vec{d} \neq 0 \\ \vec{d} \cdot \vec{a} \neq 0 \end{array} \right\} \text{No orthogonal vectors}$$

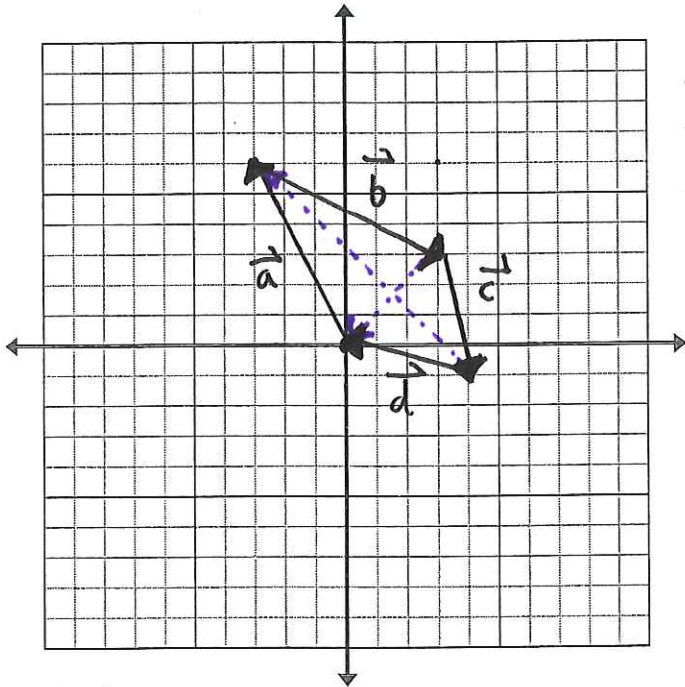
$$\left. \begin{array}{l} \vec{a} \parallel \vec{c} \\ \vec{b} \parallel \vec{d} \end{array} \right\} \text{parallel vectors}$$

SHOW ALL OF YOUR WORK.

a) Graph vectors $\vec{a} + \vec{b} + \vec{c} + \vec{d}$ when $\vec{a} = \begin{pmatrix} -3 \\ 6 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 6 \\ -3 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} 1 \\ -4 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -4 \\ 1 \end{pmatrix}$ on the graph below.

b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.

c) Classify the type of quadrilateral.



After making calculations, identify properties below:

$$|\vec{a}| = |\vec{c}|$$

$$|\vec{b}| = |\vec{d}|$$

Two distinct pairs of equal adjacent sides.

$(\vec{d} + \vec{a}) \perp (\vec{c} + \vec{b})$
The diagonals of the kite are perpendicular!

Quadrilateral

Kite!

Calculations

Magnitudes (lengths):

$$|\vec{a}| = \sqrt{(-3)^2 + (6)^2} = \sqrt{9 + 36} = \sqrt{45}$$

$$|\vec{b}| = \sqrt{(6)^2 + (-3)^2} = \sqrt{36 + 9} = \sqrt{45}$$

$$|\vec{c}| = \sqrt{1^2 + (-4)^2} = \sqrt{1 + 16} = \sqrt{17}$$

$$|\vec{d}| = \sqrt{(-4)^2 + 1^2} = \sqrt{16 + 1} = \sqrt{17}$$

Parallel or Perpendicular Vectors:

$$\vec{d} + \vec{a} = \begin{pmatrix} -7 \\ 7 \end{pmatrix}$$

$$\vec{c} + \vec{b} = \begin{pmatrix} -3 \\ -3 \end{pmatrix}$$

$$(\vec{d} + \vec{a}) \cdot (\vec{c} + \vec{b}) = 21 - 21 = 0$$

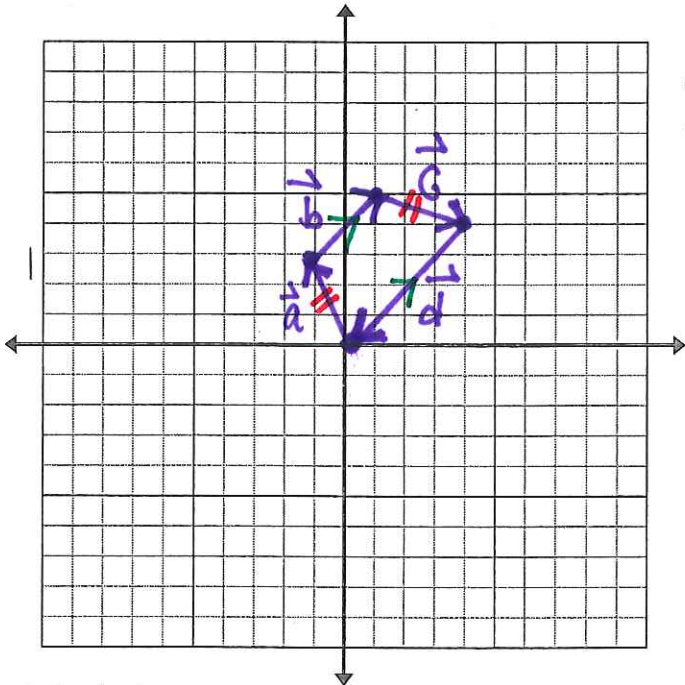
$$-7(-3) + 7(-3) = 21 - 21 = 0$$

SHOW ALL OF YOUR WORK.

a) Graph vectors $A+B+C+D$ when $\vec{a} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$, $\vec{b} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$, $\vec{c} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$, $\vec{d} = \begin{pmatrix} -4 \\ -4 \end{pmatrix}$ on the graph below.

b) Identify any properties of the quadrilateral using magnitudes (distances) and parallel/perpendicular vectors.

c) Classify the type of quadrilateral.



After making calculations, identify properties below:

Vectors \vec{b} & \vec{d} are parallel.
(One pair of parallel sides).

Quadrilateral

Isosceles
Trapezoid

Calculations

Magnitudes (lengths):

$$|\vec{a}| = \sqrt{1+9} = \sqrt{10}$$

$$|\vec{b}| = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$|\vec{c}| = \sqrt{9+1} = \sqrt{10}$$

$$|\vec{d}| = \sqrt{16+16} = \sqrt{32} = 4\sqrt{2}$$

Equal
Size

Parallel or Perpendicular Vectors:

$$\vec{b} \parallel \vec{d} \text{ because } -2\vec{b} = \vec{d}$$

$$\vec{a} \cdot \vec{b} \neq 0$$

$$\vec{b} \cdot \vec{c} \neq 0$$

$$\vec{a} \cdot \vec{d} \neq 0$$

$$\vec{c} \cdot \vec{d} \neq 0$$

No orthogonal
vectors