

Unit 8 Quiz 1

Probability

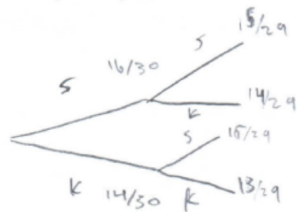
*Look over highlighted errors - this is where the mistake begins.

*Make quiz corrections... you will have an opportunity to improve this score!

"This mistake was cool!"

4. Two students each draw a piece of candy from a bag. In the bag, there are 16 Starbursts and 14 Hershey kisses. Students close their eyes and select one candy, and then eat it.

a) Create a tree diagram to model the scenario. Label probabilities on the branches and at the end of each path.



SS	$\frac{240}{870}$
SK	$\frac{224}{870}$
KS	$\frac{224}{870}$
KK	$\frac{182}{870}$

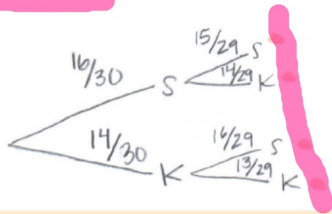
b) What is the probability that the first person and second person both choose a Hershey Kiss?

$$\frac{14}{30} \cdot \frac{14}{29} = \frac{196}{870} = \frac{98}{435}$$

"This mistake surprised me!"

4. Two students each draw a piece of candy from a bag. In the bag, there are 16 Starbursts and 14 Hershey kisses. Students close their eyes and select one candy, and then eat it.

a) Create a tree diagram to model the scenario. Label probabilities on the branches and at the end of each path.



"I loved this mistake!"

6. How many numbers greater than 5000 can you create?

a) Use digits 2,4,5,7 without repeats.

$$\frac{2 \cdot 3 \cdot 2 \cdot 1}{(\leftarrow \uparrow \text{ or } \rightarrow)} = \underline{12 \text{ numbers}}$$

b) Use digits 2, 4,5,7,9 without repeats.

$$\frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{\text{And?}} = \underline{120 \text{ numbers}}$$

(Any #, any
positive 5-digit
is greater)

Version 1

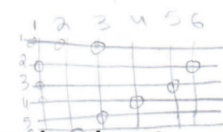
1. Jeffery is performing an experiment by rolling two dice. During his experiment he gets the following sums of rolls: 2, 5, 7, 7, 8, 9, 6, 4, 10, 11, 12, 12, 8, 4, 7, 10.

a) According to Jeffery's experiment, what is the probability of rolling a **sum of 8**?

$$\frac{2}{16} = \frac{1}{8} = .125 = 12.5\%$$

b) What is the theoretical probability of rolling a **sum of 8**?

$$\frac{5}{36} \approx 0.13\bar{8} \approx 13.8\%$$



c) What is the theoretical probability of rolling **sum of 8 or a sum less than 4**?

$$\frac{5}{36} + \frac{3}{36} = \frac{8}{36} \approx 0.22\bar{2} \approx 22\%$$

Version 1

1. Jeffery is performing an experiment by rolling two dice. During his experiment he gets the following sums of rolls: 2, 5, 7, 7, 8, 9, 6, 4, 10, 11, 12, 12, 8, 4, 7, 10.

a) According to Jeffery's experiment, what is the probability of rolling a sum of 8?

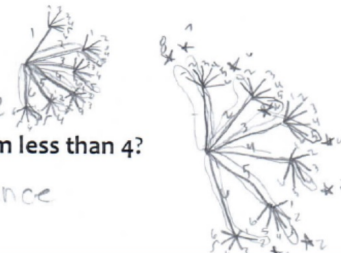
16 total rolls
2 eights
 $2/16 = 1/8 = .125 = 12.5\%$ chance of an 8

b) What is the theoretical probability of rolling a sum of 8?

2+6, 3+5, 4+4
6+2, 5+3
36 outcome
 $5/36 \approx .139 \approx 13.9\%$ chance

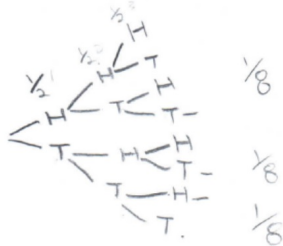
c) What is the theoretical probability of rolling sum of 8 or a sum less than 4?

$8/36 = 2/9 \approx .22 \approx 22\%$ chance



Version 1

2. Three coins are tossed. Find the probability of tossing a head and 2 tails (regardless of order).



$\frac{3}{8}$ of tossing 1 head and 2 tails

2. Three coins are tossed. Find the probability of tossing a head and 2 tails (regardless of order).



$$\frac{1}{2} * \frac{1}{2} * \frac{1}{2} = \frac{1}{8}$$

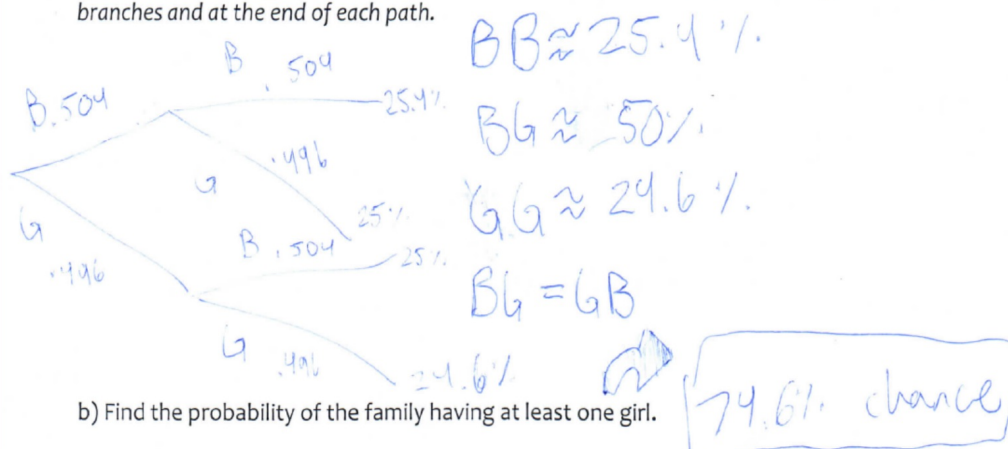
$$\frac{1}{8} + \frac{1}{8} + \frac{1}{8} = \frac{3}{8}$$

$$\frac{3}{8} \approx 37.5\% \text{ chance}$$

Version 1

3. A family will have two children. Based on the proportion of men and women in the world, the probability of a boy is 50.4% and the probability of a girl is 49.6%.

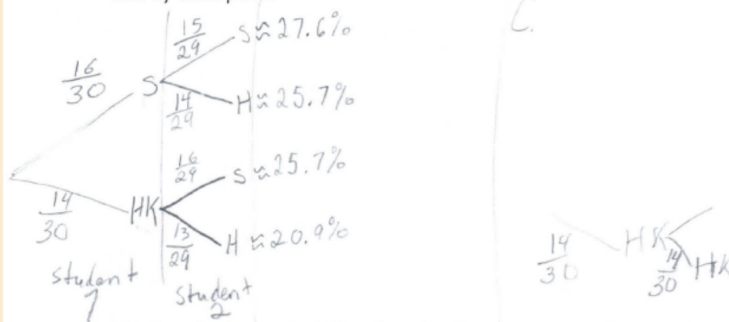
a) Create a tree diagram to model the scenario. Label probabilities in decimal form on the branches and at the end of each path.



Version 1

4. Two students each draw a piece of candy from a bag. In the bag, there are 16 Starbursts and 14 Hershey kisses. Students close their eyes and select one candy, and then eat it.

a) Create a tree diagram to model the scenario. Label probabilities on the branches and at the end of each path.



b) What is the probability that the first person **and** second person both choose a Hershey Kiss?

$$20.9\%$$

c) Consider if the first student gets a piece of candy, and then puts it back in the bag as they decide they no longer want any candy. Now, what is the probability that the first person **and** second person both choose a Hershey Kiss?

$$\frac{14}{30} \times \frac{14}{30} = 21.77\%$$

Version 1

5. State if each scenario involves a permutation or a combination. Then find the number of possibilities.

a) There are 40 applicants for 3 computer programming positions.

Combination $\frac{40!}{3!(40-3)!} = 9880$

b) The student body of 60 students wants to elect a president, vice president, secretary, and treasurer.

Permutation $\frac{60!}{(60-4)!} = 60 \cdot 59 \cdot 58 \cdot 57 \cdot 56 \cdot 55 \cdot \dots$
 11703240

5. State if each scenario involves a permutation or a combination. Then find the number of possibilities.

a) There are 40 applicants for 3 computer programming positions.

Combination $\frac{40!}{(40-3)! 3!} = \frac{40!}{37! 3!} = 9880$

b) The student body of 60 students wants to elect a president, vice president, secretary, and treasurer.

Permutation $\frac{60!}{(60-4)!} = \frac{60!}{56!} = 11703240$

Version 1

6. How many numbers greater than 5000 can you create?

a) Use digits 2,4,5,7 without repeats.

#s in the 7000's (7 followed by any permutation of the remaining #s) = 6 options, plus #s in the 5000's = 6 options for 1st digit

b) Use digits 2, 4,5,7,9 without repeats.

of 12 options $(3! + 3!) = 12$
using 4 digits = $4! + 4! + 4! = 72$ options

using all 5 digits = $5! = 120$ $120 + 72 = 192$ options

Version 1

6. How many numbers greater than 5000 can you create?

a) Use digits 2,4,5,7 without repeats.

$$\frac{2}{(\leftarrow \text{or } \rightarrow)} \cdot \frac{3}{\quad} \cdot \frac{2}{\quad} \cdot \frac{1}{\quad} = \underline{12 \text{ numbers}}$$

b) Use digits 2, 4,5,7,9 without repeats.

$$\frac{5}{\quad} \cdot \frac{4}{\quad} \cdot \frac{3}{\quad} \cdot \frac{2}{\quad} \cdot \frac{1}{\quad} = \underline{120 \text{ numbers}} \text{ and?}$$

(Any #, any positive 5-digit # is greater)

and? 4-digit values over 5000!

Version 2

1. Myles is performing an experiment by rolling two dice. During his experiment he gets the following sums of rolls: 2, 5, 7, 7, 8, 9, 6, 4, 10, 11, 12, 12, 8, 7, 7, 10.

a) According to the experiment, what is the probability of rolling a sum of 7?

$$P_e(\text{choosing } 7) = 4/16 = 1/4 = \boxed{25\%}$$

b) What is the theoretical probability of rolling a sum of 7?

$$P_t(\text{choosing } 7) = 6/36 = 1/6 \approx \boxed{17\%}$$

c) What is the theoretical probability of rolling sum of 7 or a sum less than 4?

$$P_t(\text{choosing } 1, 2, 3, \text{ or } 7) = 9/36 = 1/4 = \boxed{25\%}$$

	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

Version 2

1. Myles is performing an experiment by rolling two dice. During his experiment he gets the following sums of rolls: 2, 5, 7, 7, 8, 9, 6, 4, 10, 11, 12, 12, 8, 7, 7, 10.

a) According to the experiment, what is the probability of rolling a sum of 7?

$$4/16 \quad 1/4 \quad \text{or } 25\%$$

b) What is the theoretical probability of rolling a sum of 7?

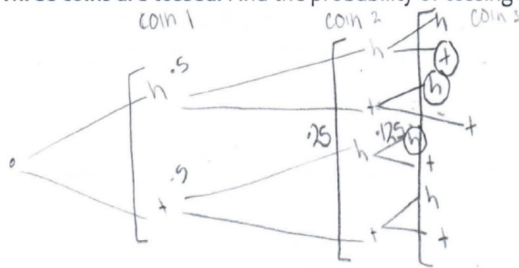
$$\begin{array}{l} 1\ 6 \\ 2\ 5 \\ 3\ 4 \end{array} \quad \begin{array}{l} 4\ 3 \\ 5\ 2 \\ 6\ 1 \end{array} \quad 6/36 \quad 1/6 \quad \text{or } 16.\bar{6}\%$$

c) What is the theoretical probability of rolling sum of 7 or a sum less than 4?

$$\begin{array}{l} 1\ 1 \\ 1\ 2 \end{array} \quad \begin{array}{l} 2\ 1 \\ 1\ 6 \end{array} \quad \begin{array}{l} 3\ 4 \\ 4\ 3 \end{array} \quad \begin{array}{l} 6\ 1 \\ 5\ 2 \end{array} \quad 9/36 \quad 3/12 \quad 1/4 \quad \text{or } 25\%$$

Version 2

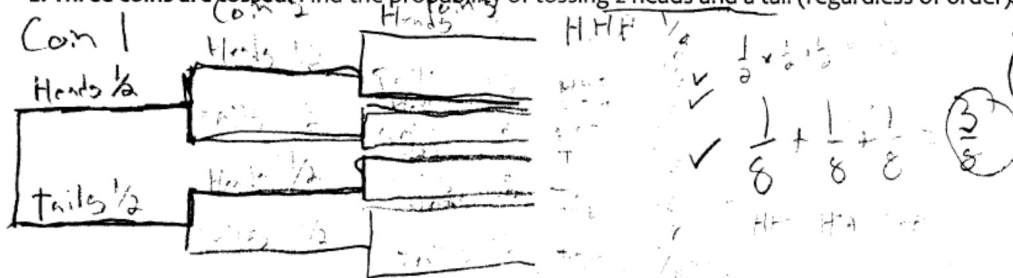
2. Three coins are tossed. Find the probability of tossing 2 heads and a tail (regardless of order).



$$0.125 \cdot 3 = 0.375 = \approx 38\%$$

of 2 heads
& 1 tail

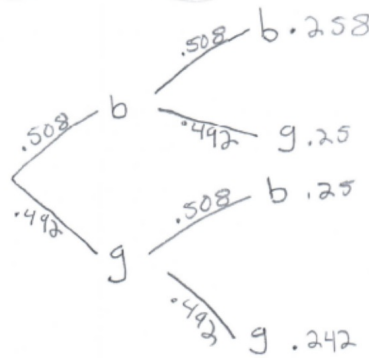
2. Three coins are tossed. Find the probability of tossing 2 heads and a tail (regardless of order).



Version 2

3. A family will have two children. Based on the proportion of men and women in the world, the probability of a boy is 50.8% and the probability of a girl is 49.2%.

a) Create a tree diagram to model the scenario. **Label probabilities in decimal form to the thousandth place (0.001) on the branches AND at the end of each path.**



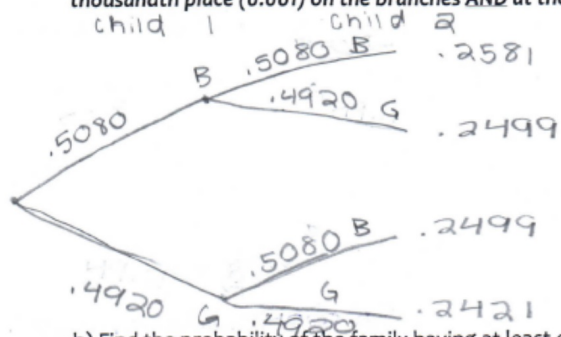
b) Find the probability of the family having at least one girl. Round to the thousandth, 0.001.

$$.25 + .25 + .242 \approx .742 \text{ or } 74.2\% \text{ chance}$$

Version 2

3. A family will have two children. Based on the proportion of men and women in the world, the probability of a boy is 50.8% and the probability of a girl is 49.2%.

a) Create a tree diagram to model the scenario. Label probabilities in decimal form to the thousandth place (0.001) on the branches AND at the end of each path.



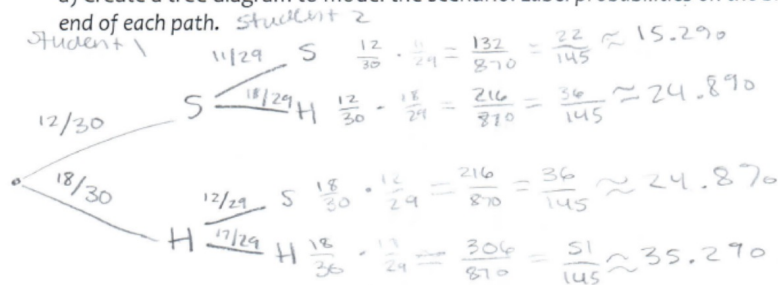
b) Find the probability of the family having at least one girl. Round to the thousandth, 0.001.

$$.2499 + .2499 + .2421 = .7419$$

Version 2

4. Two students each draw a piece of candy from a bag. In the bag, there are 12 Starbursts and 18 Hershey kisses. Students close their eyes and select one candy, and then eat it.

a) Create a tree diagram to model the scenario. Label probabilities on the branches and at the end of each path.



b) What is the probability that the first person and second person both choose a Hershey Kiss?

HH $\frac{51}{145} \approx 35.2\%$ chance both pick Hersheys

c) Consider if the first student gets a piece of candy, and then puts it back in the bag as they decide they no longer want any candy. Now, what is the probability that the first person and second person both choose a Hershey Kiss?

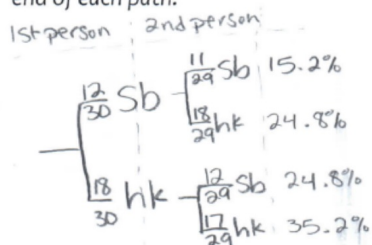
$\frac{18}{30} \cdot \frac{18}{30} = \frac{324}{900} = \frac{54}{150} = \frac{27}{75} = \frac{9}{25}$ or 36% chance they both choose Hershey

5. State if each scenario involves a permutation or a combination. Then find the number of

Version 2

4. Two students each draw a piece of candy from a bag. In the bag, there are 12 Starbursts and 18 Hershey kisses. Students close their eyes and select one candy, and then eat it. ~~without replacement~~

a) Create a tree diagram to model the scenario. Label probabilities on the branches and at the end of each path.



$$\frac{12}{30} \cdot \frac{11}{29} = \frac{132}{870} \approx 15.2\%$$

$$\frac{12}{30} \cdot \frac{18}{29} = \frac{216}{870} \approx 24.8\%$$

$$\frac{18}{30} \cdot \frac{17}{29} = \frac{306}{870} \approx 35.2\%$$

b) What is the probability that the first person **and** second person both choose a Hershey Kiss?

$$\frac{306}{870} \approx 35.2\%$$

c) Consider if the first student gets a piece of candy, and then puts it back in the bag as they decide they no longer want any candy. Now, what is the probability that the first person **and** second person both choose a Hershey Kiss?

$$\frac{18}{30} \cdot \frac{18}{30} = \frac{324}{900} = 36\%$$

Version 2

5. State if each scenario involves a permutation or a combination. Then find the number of possibilities.

a) There are 30 applicants for 3 computer programming positions.

Combination

$$\frac{30!}{(30-3)! \cdot 3!} = \frac{30 \cdot 29 \cdot 28 \cdot 27 \dots}{(27 \cdot 26 \cdot 25 \dots) \cdot 3!} = \frac{30 \cdot 29 \cdot 28}{6} = 4060$$

b) The student body of 80 students wants to elect a president, vice president, secretary, and treasurer.

Permutation

$$\frac{80!}{(80-4)!} = \frac{80 \cdot 79 \cdot 78 \cdot 77 \dots}{76 \cdot 75 \cdot 74 \dots} = 37,957,920$$

5. State if each scenario involves a permutation or a combination. Then find the number of possibilities.

a) There are 30 applicants for 3 computer programming positions.

SAME JOB
COMBINATION

$$\frac{n!}{(n-r)! \cdot r!} = \frac{30!}{(30-3)! \cdot 3!} = \frac{30!}{27! \cdot 3!} = 4060 = 30 C 3$$

30 C 3 = 4060 POSSIBILITIES

b) The student body of 80 students wants to elect a president, vice president, secretary, and treasurer.

PERMUTATION
DIFFERENT JOBS

$$\frac{80!}{(80-4)!} = \frac{80!}{76!} = 80 \cdot 79 \cdot 78 \cdot 77 = 80 P 4$$

80 P 4 = 37,957,920 POSSIBILITIES

Version 2

6. How many numbers greater than 5000 can you create?

$$= 3,795,7920$$

a) Use digits 2,5,8,9 without repeats.

2 can go here

$$\frac{4}{d_1} \cdot \frac{3}{d_2} \cdot \frac{2}{d_3} \cdot \frac{1}{d_4} = 24$$

2589
2859
2598
2895
2985
2958

6 possibilities under 5000

$$24 - 6 = 18$$

18 numbers

b) Use digits 2,5,6,8,9 without repeats.

all over 5000

$$\frac{5}{d_1} \cdot \frac{4}{d_2} \cdot \frac{3}{d_3} \cdot \frac{2}{d_4} \cdot \frac{1}{d_5} = 5! = 120$$

120 numbers

and?

and? 4-digit values over 5000!